

Introduction
to
Formal Methods (Part I)

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A couple of reasons to be rigorous

[\[https://www.omg.org/spec/BPMN/2.0/\]](https://www.omg.org/spec/BPMN/2.0/)

A converging **Inclusive Gateway** is used to merge a combination of alternative and parallel paths. A control flow *token* arriving at an **Inclusive Gateway** MAY be synchronized with some other *tokens* that arrive later at this **Gateway**. **The precise synchronization** behavior of the **Inclusive Gateway** **can be found on page 292.**

292

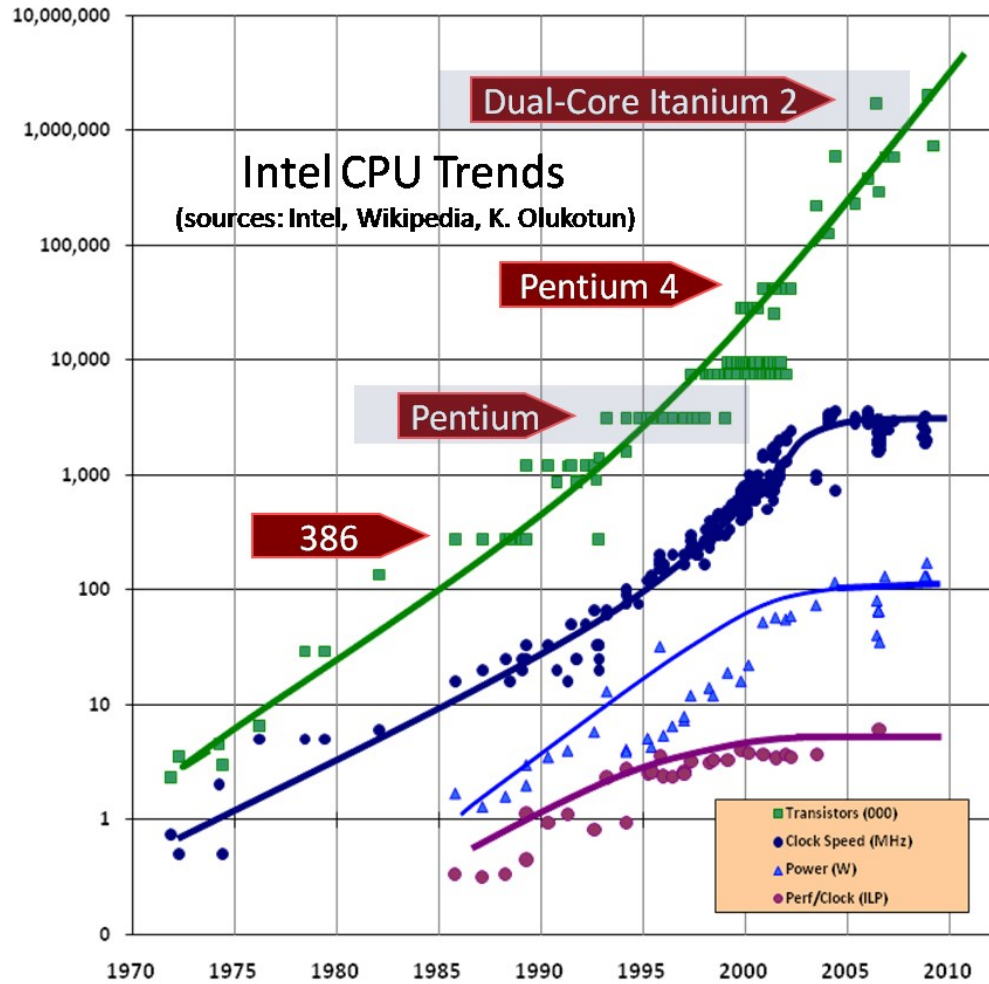
Business Process Model and Notation, v2.0

[\[https://stackoverflow.com/questions/1812990/incrementing-in-c-when-to-use-x-or-x\]](https://stackoverflow.com/questions/1812990/incrementing-in-c-when-to-use-x-or-x)

The screenshot shows the Stack Overflow website interface. At the top, there is a navigation bar with the Stack Overflow logo, links for 'About', 'Products', and 'For Teams', and a search bar. Below the navigation bar is a sidebar with a 'Home' link and a 'PUBLIC' section containing 'Questions', 'Tags', 'Users', and 'Companies'. Underneath is a 'COLLECTIVES' section. The main content area features a question titled 'Incrementing in C++ - When to use x++ or ++x?' with a sub-header 'Asked 12 years, 11 months ago Modified 1 year, 1 month ago Viewed 251k times'. The question body contains two paragraphs: the first starts with 'I'm currently learning C++ and I've learned about the incrementation a while ago. I know that you can use "++x" to make the incrementation before and "x++" to do it after.' and the second starts with 'Still, I really don't know when to use either of the two... I've never really used "++x" and things always worked fine so far - so, when should I use it?'. On the right side of the question, there is a 'The Overflow' sidebar with two items: 'Making new da' and 'Stop re test: M'.

A reason to go concurrent

[<https://i.extremetech.com/imagery/content-types/03zc6ghfKswe41smvPXi8Zh/images-6.jpg>]



[<https://www.comsol.com/blogs/havent-cpu-clock-speeds-increased-last-years>]

COMSOL Blog

Why Haven't CPU Clock Speeds Increased in the Last Few Years?

by Pär Persson Mattsson

November 13, 2014

Categories: [COMSOL Now](#)

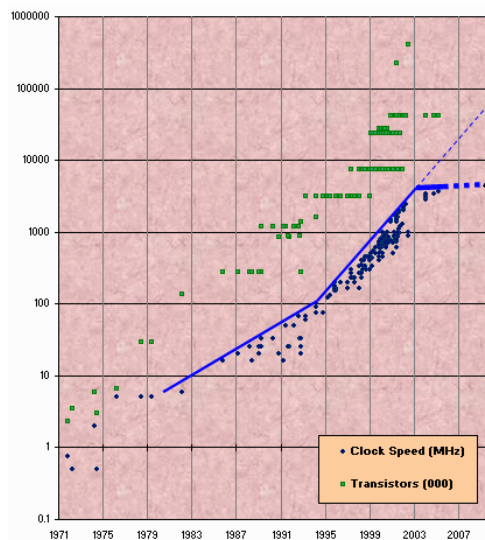
Get New Posts by Email

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The first computer I used was a real performance beast. Equipped with Intel's 486 clocking in at

the art - multi-processor programming

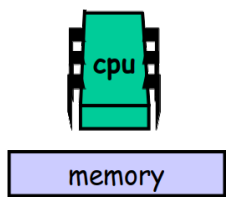
Hw Efficiency is no longer an "hw thing" → SW



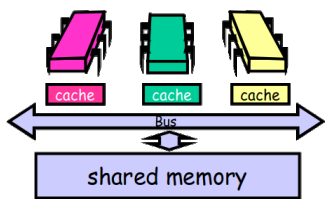
clock speed

transistors grow by a factor of 10 every 10 years!

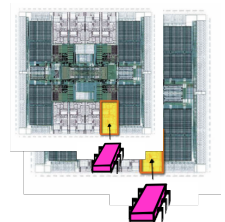
CPU speed is plateauing



uni processor



shared-memory processor



multicore

programming constructs everywhere

- "new" languages
 - Cobol
 - Scala
 - Erlang/Elixir
 - Ballerina
 - Goroutines

libraries (AKKA)

Modelling languages

- BPEL
- BPMN

Job interviews and prime numbers

print

"On the first day of your new job, your boss asks you to ~~find~~ all primes between 1 and 10^{10} (never mind why), using a parallel machine that supports ten concurrent threads. This machine is rented by the minute, so the longer your program takes, the more it costs. You want to make a good impression. What do you do?"


[Herlihy, Shavit: The Art of Multiprocessor Programming. Elsevier, 2012.]

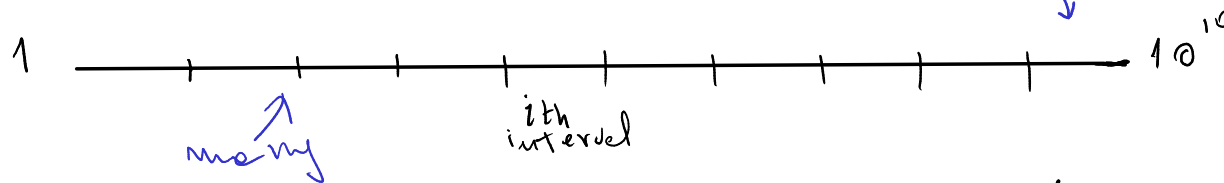
An example of shared memory concurrency

Printing all the prime numbers below 10^{10} ... sequentially

```
1 void primeSeq {  
2   for (j = 1, j < 10^10; j++) {  
3     if (isPrime(j))  
4       print(j);  
5   }  
6 }
```

Now let's try concurrently

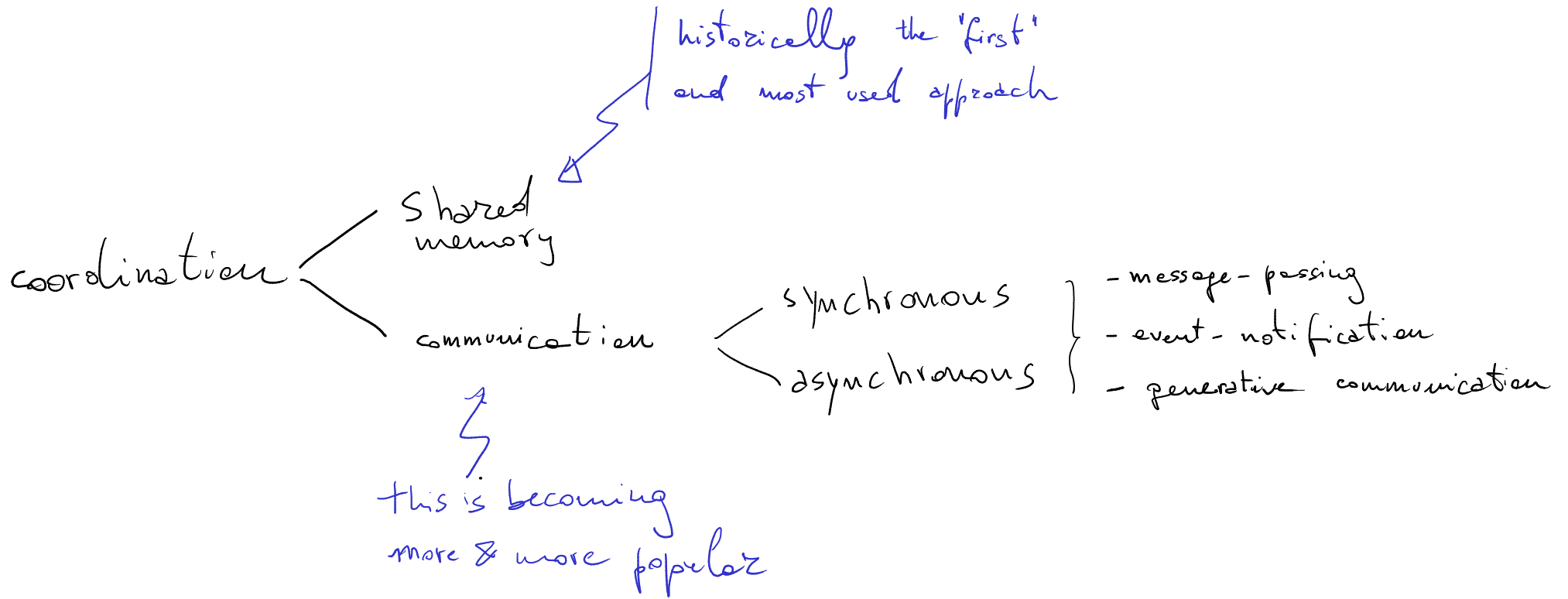
 Split the interval & launch a thread on each position
primes are distributed unevenly



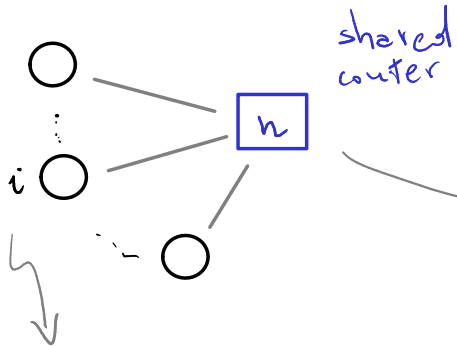
```
void primePrint(int i){ // i non-negative  
  for (j = i*10^9+1, j < (i+1)*10^9; j++) {  
    if (isPrime(j))  
      print(j);  
  }  
}
```

How good is this idea?

- o uneven load
- o should we look for an optimal split?



Exercise 0 Find a better multi-threaded program for printing the first 10^{10} primes



```
void primePrint( Counter counter ) {
    long j = 0;
    while (j < 10^10) {
        j = counter.getAndIncrement();
        if (isPrime(j))
            print(j);
    }
}
```

```
public class Counter {
    private long value;

    public long getAndIncrement() {
        return value++;
    }
}
```

THIS IS NOT GOOD!
RACES
synchronised!

temp := value
value ++
return temp

```
public long getAndIncrement() {
    synchronized {
        temp = value;
        value = temp + 1;
    }
    return temp;
}
```

even better
WHY?

REFLECT about why this solution is better than splitting

Some terminology

Concurrency vs Parallelism

compose "independent" stuff

deal with a lot of stuff
AT ONCE

GOAL: "good" composition

run stuff simultaneously

do a lot of stuff
AT ONCE

GOAL: "good" execution

DESIGN

PERFORMANCE

break down problems
&
compose the solutions