

Immigration Course
on
Formal Methods

Academic year 2023/2024

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A couple of reasons to be rigorous

[<https://www.omg.org/spec/BPMN/2.0/>]

A converging **Inclusive Gateway** is used to merge a combination of alternative and parallel paths. A control flow *token* arriving at an **Inclusive Gateway** MAY be synchronized with some other *tokens* that arrive later at this **Gateway**. **The precise synchronization** behavior of the **Inclusive Gateway** can be found on page 292.

292

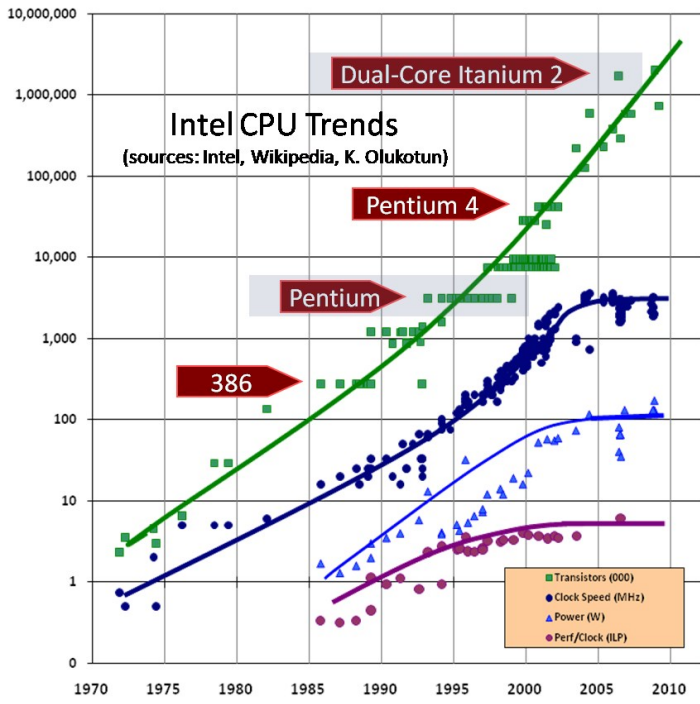
Business Process Model and Notation, v2.0

[<https://stackoverflow.com/questions/1812990/incrementing-in-c-when-to-use-x-or-x>]

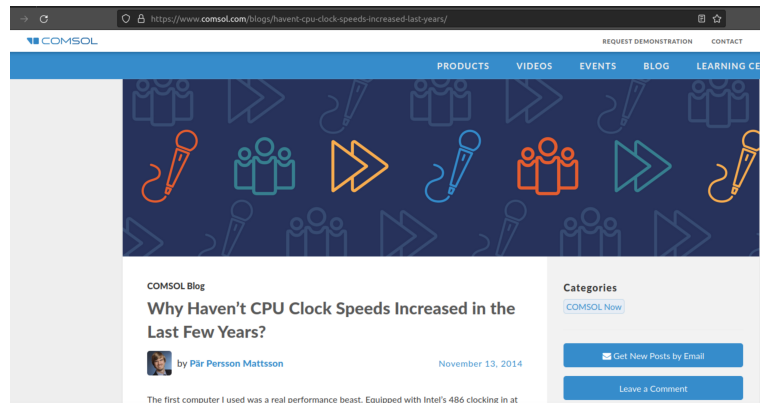
The screenshot shows a Stack Overflow page for the question "Incrementing in C++ - When to use x++ or ++x?". The page includes a navigation bar with "stackoverflow", "About", "Products", "For Teams", and a search bar. A left sidebar contains links for "Home", "PUBLIC", "Questions", "Tags", "Users", "Companies", and "COLLECTIVES". The main content area shows the question title, its status as "PUBLIC", and its statistics: "Asked 12 years, 11 months ago", "Modified 1 year, 1 month ago", and "Viewed 251k times". There are two answers visible. The first answer, marked as the top answer with an upvote arrow, has 118 votes and reads: "I'm currently learning C++ and I've learned about the incrementation a while ago. I know that you can use \"++x\" to make the incrementation before and \"x++\" to do it after." The second answer, marked with a downvote arrow, has 0 votes and reads: "Still, I really don't know when to use either of the two... I've never really used \"++x\" and things always worked fine so far - so, when should I use it?". On the right side, there is a "The Overflow" sidebar with two items: "Making new da" and "Stop re test: M".

A reason to go concurrent

[<https://i.extremetech.com/imagery/content-types/03zc6ghfKswe41smvPXi8Zh/images-6.jpg>]

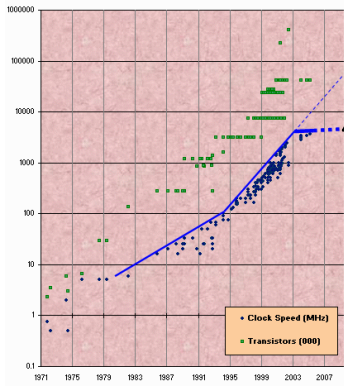


[<https://www.comsol.com/blogs/havent-cpu-clock-speeds-increased-last-years/>]



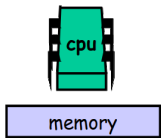
the art - multi-processor programming

Hw $\xrightarrow{\text{Efficiency is no longer on hw thing}}$ Sw

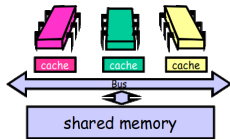


clock speed
 # transistors grows by a factor of 10 every 10 years
 CPU speed is plateauing

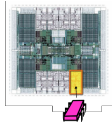
- programming constructs in all languages
- "new" languages
 - Go
 - Scala
 - Elixir / Erlang
 - Ballerina
 - Concurus
- supporting library, AKKA
- Modelling languages
 - BPEL
 - BPMN



uniprocessor



shared memory processor



multicore

Job interviews and prime numbers

"On the first day of your new job, your boss asks you to find all primes between 1 and 10^{10} (never mind why), using a parallel machine that supports ten concurrent threads. This machine is rented by the minute, so the longer your program takes, the more it costs. You want to make a good impression. What do you do?"

[Herlihy, Shavit: The Art of Multiprocessor Programming. Elsevier, 2012.]

An example of shared memory concurrency

Print all prime integers between 1 & 10^{10}

```
1 void primeSeq {  
2   for (j = 1, j < 10^10; j++) {  
3     if (isPrime(j))  
4       print(j);  
5   }  
6 }
```

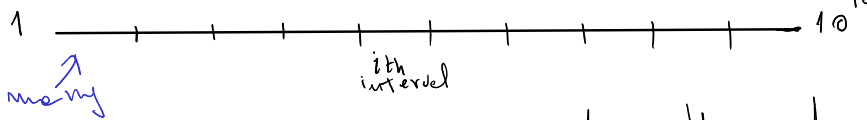
Now let's try concurrently



Split the interval & launch a thread on each position

primes are distributed unevenly

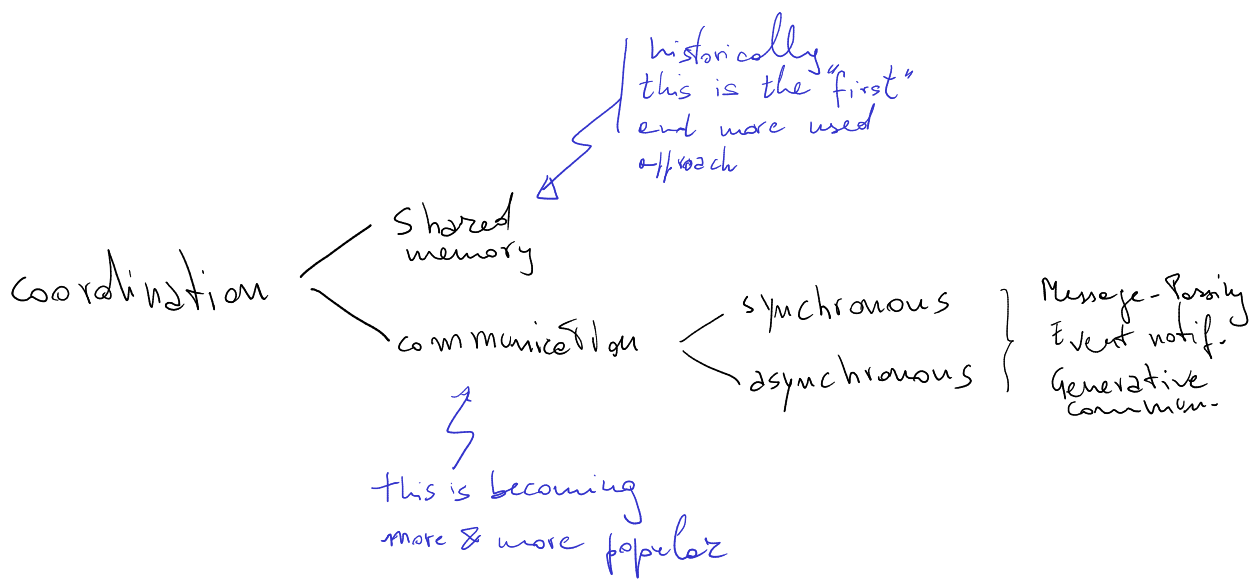
few



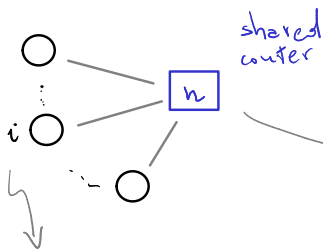
```
void primePrint(int i) { // i non-negative  
  for (j = i*10^9+1, j < (i+1)*10^9; j++) {  
    if (isPrime(j))  
      print(j);  
  }  
}
```

How good is this idea?

- uneven load
- Is there an "optimal" split?



Exercise 0 Find a better multi-threaded program for the primality test



```
void primePrint( Counter counter ) {  
    long j = 0;  
    while (j < 10^10) {  
        j = counter.getAndIncrement();  
        if (isPrime(j))  
            print(j);  
    }  
}
```

```
public class Counter {  
    private long value;  
    public long getAndIncrement() {  
        return value++;  
    }  
}
```

RACES
synchronised!

THIS IS NOT GOOD!

temp := value
value ++
return temp

even better
WHY?

```
public long getAndIncrement() {  
    synchronized {  
        temp = value;  
        value = temp + 1;  
    }  
    return temp;  
}
```

REFLECT about why this solution is better than splitting

Some terminology

Concurrency vs Parallelism

compose "independent" stuff
deal with a lot of stuff
AT ONCE

run stuff simultaneously
do a lot of stuff
AT ONCE

GOAL: "good" composition

GOAL: "good" execution

DESIGN

PERFORMANCE

break down problems
&
compose the pieces

A Choreographic Formal Model of Communicating Systems
—Immigration Course on Formal Methods—

Emilio Tuosto @ GSSI

So far...

- An idea of FMs

Leonardo da Vinci

“ Ma prima farò alcuna esperienza avanti ch'io più oltre proceda, perché mia intenzione è allegare prima l'esperienza e poi colla ragione dimostrare. ”

eM's (bad) translation

“ Before proceeding further, I will first get some experiment, because my intention is to first understand the experiment and then to explain it with the intellect. ”

- Concurrency vs Parallelism
- Shared-memory

Message-passing

Pink Floyd

"Is there anybody out there?"

A glimpse of Erlang

```
ping(N, Pong_PID) ->
  Pong_PID ! {ping, self()},
  receive
    pong ->
      io:format("Ping received pong~n", [])
  end,
  ping(N - 1, Pong_PID).

ping(0, Pong_PID) ->
  Pong_PID ! finished,
  io:format("ping finished~n", []).

pong() ->
  receive
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```

Semantics

- Message passing
- FIFO buffers [mailboxes in Erlang's jargon]
- Spawn of threads

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Asynchrony by design

Erlang is an embodiment of the well-known actor model of Hewitt and Agha...dates back to '73!

Friendlier representations

Local behaviour: communicating machines



CFSMs (Brand & Zafiropulo 1983!): FIFO buffers as well

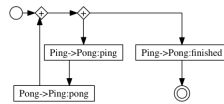
Friendlier representations

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Choreography: global graph



...“synchronous” distributed workflow (Deniérou and Yoshida 2012)

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Q:
Is this program correct?

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Q:

Is this program correct?

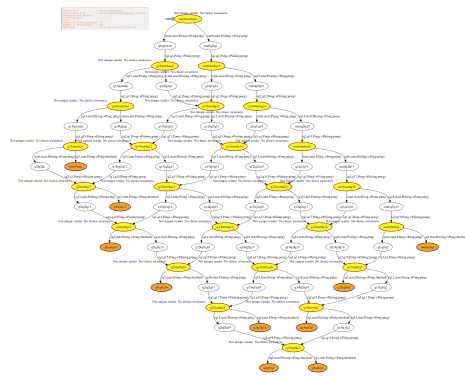
A:




No!

Exercise:

find the bug

Send ping-pong to shell !!! ... I mean, use ChoSyn



-  [Brand, D. and Zafiropulo, P. \(1983\).](#)
On Communicating Finite-State Machines.
JACM, 30(2):323–342.
-  [Guanciale, R. and Tuosto, E. \(2016\).](#)
An abstract semantics of the global view of choreographies.
In *Proceedings 9th Interaction and Concurrency Experience, ICE 2016, Heraklion, Greece, 8-9 June 2016.*, pages 67–82.
-  [Tuosto, E. and Guanciale, R. \(2018\).](#)
Semantics of global view of choreographies.
Journal of Logic and Algebraic Methods in Programming, 95:17–40.
Revised and extended version of [Guanciale and Tuosto, 2016].